

$$\begin{aligned} \# 46 \quad & \log 12 + \frac{1}{2} \log 7 - \log 2 \\ &= \log 12 + \log 7^{1/2} = \log 2 \\ &= \log \frac{\cancel{12} \sqrt{7}}{\cancel{2}} \\ &= \log (6\sqrt{7}) \end{aligned}$$

$$\begin{aligned} \# 48. \quad & \underbrace{\log_5 x + \log_5 (x+1)} = \log_5 20 \\ & \log_5 \underbrace{(x^2 + x)} = \log_5 \underbrace{20} \end{aligned}$$

$$x^2 + x = 20$$

$$x^2 + x - 20 = 0$$

$$(x + 5)(x - 4) = 0$$

$$\cancel{x = -5} \text{ or } \boxed{x = 4}$$

$$\#47. \quad \underbrace{\log x + \log(x-1)} = \log 4x$$
$$\log(\underline{x^2 - x}) = \log(\underline{4x})$$

$$x^2 - x = 4x$$

$$x^2 - 5x = 0$$

$$\underline{x}(x - 5) = 0$$

$$\cancel{x=0} \text{ or } \boxed{x=5}$$

$$\#13. \quad \underbrace{\log_2 6 - \log_2 15 + \log_2 20}$$

$$\log_2 \left( \frac{6}{15} \right) + \log_2 20$$

$$\log_2 \left( \frac{\overset{2}{\cancel{6}} \cdot \overset{4}{\cancel{20}}}{\underset{\cancel{3}}{15}} \right) = \log_2 8 = 3$$

$$\begin{aligned}\#31. \ln \sqrt{ab} &= \ln (ab)^{1/2} = \frac{1}{2} \ln (ab) \\ &= \frac{1}{2} [\ln a + \ln b]\end{aligned}$$

$$\begin{aligned}\#32. \ln \sqrt[3]{3r^2s} &= \ln (3r^2s)^{1/3} \\ &= \frac{1}{3} \ln (3 \cdot r^2 \cdot s) \\ &= \frac{1}{3} [\ln 3 + 2 \ln r + \ln s]\end{aligned}$$

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## Exponential Equations

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$$x^2 = 9 \leftarrow \text{not exponential}$$

$$2^x = 9 \leftarrow \text{exponential (variable in exponent)}$$

$$\ln 2^x = \ln 9$$

$$\frac{x \cdot \cancel{\ln 2}}{\cancel{\ln 2}} = \frac{\ln 9}{\ln 2}$$

$$\rightarrow \boxed{x = \frac{\ln 9}{\ln 2}}$$

$$\text{Ex. } 3^{x+1} = 4^{2x-1}$$

$$\ln 3^{x+1} = \ln 4^{2x-1}$$

$$(x+1) \ln 3 = (2x-1) \ln 4$$

$$\log a^b = b \cdot \log a$$

$$\underline{x \ln 3 + \ln 3} = \underline{2x \ln 4 - \ln 4} \leftarrow \text{distr.}$$

$$x \ln 3 - 2x \ln 4 = -\ln 4 - \ln 3$$

$$\frac{x (\ln 3 - 2 \ln 4)}{\ln 3 - 2 \ln 4} = \frac{-\ln 4 - \ln 3}{\ln 3 - 2 \ln 4}$$

$$x = \frac{-\ln 4 - \ln 3}{\ln 3 - 2 \ln 4}$$

$$\text{Ex. } 8^{2x} = 4^{x+3}$$

$$2x \ln 8 = (x+3) \ln 4$$

$$\underline{2x \ln 8} = \underline{x \ln 4} + 3 \ln 4$$

$$2x \ln 8 - x \ln 4 = 3 \ln 4$$

$$x (2 \ln 8 - \ln 4) = 3 \ln 4$$

$$x = \frac{3 \ln 4}{2 \ln 8 - \ln 4}$$

Try Again

$$(a^m)^n = a^{mn}$$

$$8^{2x} = 4^{x+3}$$

$$(2^3)^{2x} = (2^2)^{x+3}$$

$$2^{6x} = 2^{2x+6}$$

$$6x = 2x + 6$$

$$4x = 6$$

$$\rightarrow \boxed{x = \frac{3}{2}}$$

$$\text{Ex } e^{2x} - e^x - 6 = 0$$

$$(e^x + 2)(e^x - 3) = 0$$

$$e^x + 2 = 0 \quad \text{or} \quad e^x - 3 = 0$$

$$e^x = -2$$

$$e^x = 3$$



$$\ln e^x = \ln 3$$

~~x~~

$$\boxed{x = \ln 3}$$

Alternative

$$e^{2x} - e^x - 6 = 0$$

$$y = e^x$$

$$y^2 - y - 6 = 0$$

$$(y + 2)(y - 3) = 0$$

$$y = -2 \quad \text{or} \quad y = 3$$

$$e^x = -2 \quad \text{or} \quad e^x = 3$$

$$\text{Ex : } e^x - 12e^{-x} - 1 = 0$$

$$e^x [e^x - 12e^{-x} - 1] = e^x [0]$$

$$e^{2x} - 12 - e^x = 0$$

$$\underline{e^{2x} - e^x - 12 = 0}$$

$$(e^x + 3)(e^x - 4) = 0$$

$$\underbrace{e^x + 3 = 0}_{\text{no sol.}} \quad \text{or} \quad e^x - 4 = 0$$

$$e^x = 4$$

$$\boxed{x = \ln 4}$$

HW

p. 338 # 3, 9, 13, 21, 22, 23

29, 31

give an exact  
answer in terms  
of natural logs

#9.  $3e^x = 10$

$$e^x = \frac{10}{3}$$

$$x = \ln\left(\frac{10}{3}\right)$$