

$$\boxed{\uparrow C} \neq \underline{1k}$$

$$\lim_{n \rightarrow \infty} \frac{\sum_{k=0}^n (2k-1)}{2n^2+1} = \lim_{n \rightarrow \infty} \frac{\overbrace{(n+1)(2n-2)}^{2n^2}}{2 \overbrace{(n^2+1)}^{4n^2}} = \frac{1}{2}$$

Numerator: $\sum_{k=0}^n (2k-1) = -1 + 1 + 3 + \dots + (2n-1)$
 $= \frac{n+1}{2} (2n-2)$

$$\underline{\#1k} \quad \sum_{k=0}^n 2^{k-1} = \frac{1}{2} + 1 + 2 + \dots + 2^{n-1}$$
$$= \frac{\frac{1}{2}(1-2^n)}{1-2} = \frac{1}{2}(2^n-1)$$

$$\lim_{n \rightarrow \infty} \frac{\frac{1}{2}(2^n-1)}{3^n} = 0$$

ID #2C

$$y = \frac{3x+1}{x+1}$$

$$x\text{-int } -\frac{1}{3}$$

$$y\text{-int } 1$$

$$VA \underline{x = -1}$$

$$HA \underline{y = 3}$$

$$y(-2) = \frac{-6+1}{-1}$$

$$x < -2$$

$$y(-2) = \text{---}$$

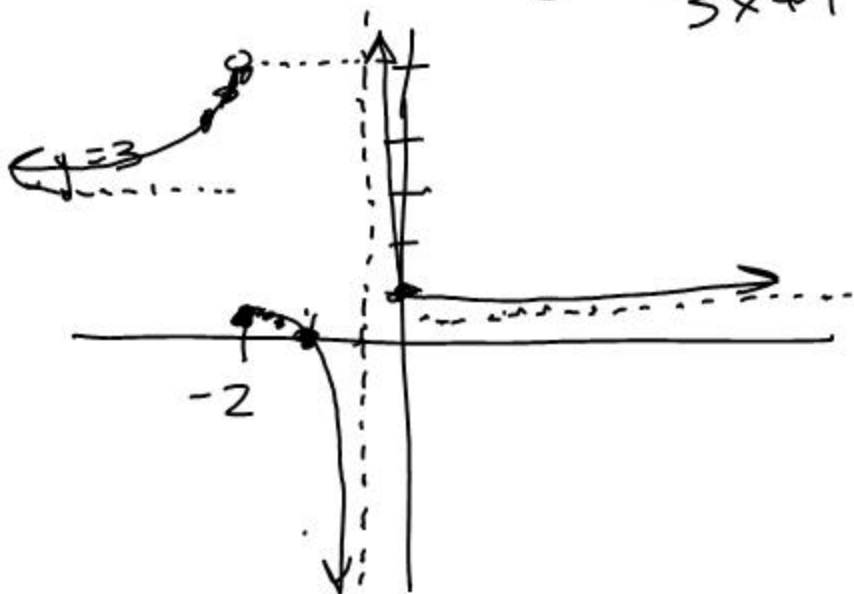
$$y = \frac{x+1}{3x+1}$$

$$x\text{-int } -\frac{1}{3}$$

$$y\text{-int } 1$$

$$VA \underline{x = -\frac{1}{3}}$$

$$HA \underline{y = \frac{1}{3}}$$



$$\lim_{x \rightarrow -2^-} f(x) = 5$$

$$\lim_{x \rightarrow -2^+} f(x) = \frac{1}{5}$$

$$\lim_{x \rightarrow -2} f(x) \text{ dne}$$

Row #1e

$$\lim_{n \rightarrow \infty}$$

$$\frac{1+2+3+\dots+2n}{n^2}$$

$$= \lim_{n \rightarrow \infty}$$

$$\frac{\boxed{2n^2}}{\boxed{n^2}} (1+2n)$$

$$= 2$$

$$f \quad 2 \sum_{k=1}^n \ln 3^k = 2 \cdot \frac{3(1-3^n)}{1-3}$$

$$= 3(3^n - 1)$$

$$\lim_{n \rightarrow \infty} \frac{3(3^n - 1)}{5^n} = 0$$

$$\lim_{x \rightarrow \infty} \frac{x^3}{2^x} \stackrel{\text{L'Hôpital's Rule}}{=} \lim_{x \rightarrow \infty} \frac{3x^2}{2^x \cdot \ln 2}$$

$\frac{\infty}{\infty}$ indeterminate form $\frac{\infty}{\infty}$

$$= \lim_{x \rightarrow \infty} \frac{6x}{2^x (\ln 2)^2} = \lim_{x \rightarrow \infty} \frac{6}{2^x (\ln 2)^3}$$

$$\frac{\infty}{\infty} \rightarrow = 0$$

L'Hospital

$$\lim_{n \rightarrow \infty} \left(1 - \frac{3}{n}\right)^{2n} = \underline{e^{-6}}$$

$a \cdot \ln b = \ln b^a$



$$\lim_{n \rightarrow \infty} \ln \left(1 - \frac{3}{n}\right)^{2n} = \lim_{n \rightarrow \infty} \underbrace{2n}_{\infty} \cdot \underbrace{\ln \left(1 - \frac{3}{n}\right)}_{0}$$

$$= \lim_{n \rightarrow \infty} \frac{2 \ln \left(1 - \frac{3}{n}\right)}{\frac{1}{n}}$$

$\frac{0}{0}$ (boxed with arrow)

$-3n^{-1}$ (above the derivative of the numerator)

$\frac{2}{(1 - \frac{3}{n})^2} \cdot \frac{3}{n^2}$ (circled with arrow)

$-\frac{1}{n^2}$ (below the derivative of the denominator)

$\frac{2}{n^{-1}}$ (below the original fraction)

$\stackrel{L'H}{=} \lim_{n \rightarrow \infty} \frac{2}{(1 - \frac{3}{n})^2} \cdot \frac{3}{n^2}$

$$= -6$$

Ex. $\lim_{x \rightarrow \infty} x \cdot \tan\left(\frac{1}{x}\right) = \lim_{x \rightarrow \infty} \frac{\tan \frac{1}{x}}{\frac{1}{x}}$

$\infty \cdot 0$ \nearrow

$\frac{0}{0}$ \nearrow

$$\frac{1}{x} = x^{-1}$$

$$-x^{-2} = -\frac{1}{x^2}$$

L'H $\lim_{x \rightarrow \infty} \frac{\sec^2\left(\frac{1}{x}\right) \cdot -\frac{1}{x^2}}{-\frac{1}{x^2}}$

$= 1$

Ex $\lim_{x \rightarrow \infty} (\sqrt{x^2 - x} - x)$ $\frac{\sqrt{x^2 - x} + x}{\sqrt{x^2 - x} + x}$

$\infty - \infty$ \nearrow

$= \lim_{x \rightarrow \infty} \frac{-x}{\sqrt{x^2 - x} + x}$

$\frac{-\infty}{\infty}$ \nearrow

$= \lim_{x \rightarrow \infty} \frac{-1}{\frac{1}{2}(x^2 - x)^{-1/2} \cdot (2x - 1) + 1}$

$$\lim_{x \rightarrow \infty} \frac{-1}{\frac{2x-1}{2(x^2-x)} + \frac{2(x^2-x)}{2(x^2-x)}}$$

$$= \lim_{x \rightarrow \infty} \frac{-2(x^2-x)}{2x^2-1} = \lim_{x \rightarrow \infty} \frac{-2x^2+2x}{2x^2-1} = -1$$