

10E #86

$$3(0.3)^3 = 3(0.027) = 0.081$$

10F #2. $Y \sim P_0(3)$

$$\begin{aligned} \text{a) } P(Y=3) &= \text{poisson pdf}(3, 3) \\ &= 0.224 \end{aligned}$$

$$\begin{aligned} \text{(b) } P(X < 3) &= P(X \leq 2) \\ &= \text{poissoncdf}(3, 2) \\ &= 0.423 \end{aligned}$$

$$\begin{aligned} \text{(c) } P(X > 3) &= 1 - P(X \leq 3) \\ &= 1 - \text{poissoncdf}(3, 3) \\ &= 0.353 \end{aligned}$$

$$\begin{aligned} \text{(d) } P(Y=4 | Y > 3) &= \frac{P(Y=4 \cap Y > 3)}{P(Y > 3)} \\ &= \frac{\text{poisson pdf}(3, 4)}{1 - \text{poissoncdf}(3, 3)} \\ &= 0.476 \end{aligned}$$

$$\boxed{100} \# 7c$$

$$5 \underbrace{(0.45)^3 (0.55)^4}_{SMT}$$

$$\boxed{100} \# 2.$$

(a) $X =$ number of flaws in 100 sq. meters

$$X \sim P_0(1)$$

$$P(X=2) = \text{poisson pdf}(1, 2) \\ = 0.184$$

(b) $Y =$ number of flaws in 25 sq. meters

$$Y \sim P_0(0.25)$$

$$P(Y \geq 1) = 1 - P(Y=0) \\ = 1 - \text{poisson pdf}(0.25, 0)$$

10E *1 $X \sim B(8, 0.4)$

(d) $\mu = E(X) = np$

$$\mu = 8(0.4) = 3.2$$

(e) $\sigma^2 = \text{Var}(X) = npq$

$$\sigma^2 = 8(0.4)(0.6) =$$

For the Poisson distribution

$$\begin{aligned} \mu &= E(X) = m \\ \sigma^2 &= \text{Var}(X) = m \end{aligned}$$

10E 2(d) $Y \sim B(7, 0.3)$

Binomial

Variance

$$\text{Var}(X) = E(X^2) - [E(X)]^2$$

10 # # 46

$$3.5 = E(X^2) - [3.5]^2$$

$$E(X^2) = 15.75$$

$$P(X=x) = \frac{e^{-m} m^x}{x!}$$

#5 $X \sim P_0(m)$ Find m :

$$P(X=0) + P(X=1) - P(X=4) = 0$$

$$\frac{e^{-m} \cdot m^0}{0!} + \frac{e^{-m} \cdot m}{1!} - \frac{e^{-m} \cdot m^4}{4!} = 0$$

$$e^{-m} \left(1 + m - \frac{m^4}{24} \right) = 0$$

Discrete Distributions

Ex.

x	0	1	2	3
$P(X=x)$	0.2	0.2	0.4	0.2

Find the mean and variance.

$$E(X) = \cancel{(0.2)(0)} + (0.2)(1) + (0.4)(2) + (0.2)(3) \\ = 1.6$$

$$E(X) = \sum x \cdot P(X=x)$$

$$\text{Var}(X) = E(X^2) - [E(X)]^2$$

$$E(X^2) = \cancel{(0.2)(0^2)} + (0.2)(1^2) + (0.4)(2^2) + \\ = 3.6 \qquad (0.2)(3^2)$$

$$\text{Var}(X) = 3.6 - (1.6)^2 = 1.04$$

Find the standard deviation.

$$\sigma = \sqrt{1.04} = 1.02$$

Find $P(X \leq 2) = 0.8$

Find the median of the distribution.

$$\boxed{\sqrt{1.5}}$$

\boxed{HW} $\boxed{10A}$ # 1-3

$\boxed{10B}$ # 1-2, 5

$\boxed{10C}$ # 1-2

$\boxed{10H}$ # 6