

Expand $(x-r_1)(x-r_2)(x-r_3)$

$$= x^3 + x^2(-r_1 - r_2 - r_3) + x(r_1 r_2 + r_1 r_3 + r_2 r_3) - r_1 r_2 r_3$$

3C

1a

$$x^2 - 3x + 2 = 0$$

$$\frac{2}{x_1} + \frac{2}{x_2}$$

$$= \frac{2x_2}{x_1 x_2} + \frac{2x_1}{x_1 x_2} = \frac{2(x_1 + x_2)}{x_1 x_2}$$

$$= \frac{2(3)}{2} = 3$$

$$(h) \quad 7x^2 + 4x - 5 = 0 \rightarrow x^2 + \left(\frac{4}{7}\right)x - \frac{5}{7} = 0$$

$$(x_1 - x_2)^4 = (x_1 - x_2)(x_1 - x_2)(x_1 - x_2)(x_1 - x_2)$$

$$= x_1^4 + 4x_1^3(-x_2) + 6x_1^2(-x_2)^2 + 4x_1(-x_2)^3 + (-x_2)^4$$

$$(x_1 - x_2)^4 =$$

$$= x_1^4 - 4x_1^3x_2 + 6x_1^2x_2^2 - 4x_1x_2^3 + x_2^4$$

$$(x_1 + x_2)^4 = x_1^4 + 4x_1^3x_2 + 6x_1^2x_2^2 + 4x_1x_2^3 + x_2^4$$

$$(x_1 - x_2)^4 = (x_1 + x_2)^4 - 8x_1^3x_2 - 8x_1x_2^3$$

$$= (x_1 + x_2)^4 - 8x_1x_2[x_1^2 + x_2^2]$$

$$= (x_1 + x_2)^4 - 8x_1x_2[(x_1 + x_2)^2 - 2x_1x_2]$$

$$= \left(-\frac{4}{7}\right)^4 - 8\left(-\frac{5}{7}\right)\left[\left(\frac{4}{7}\right)^2 - 2\left(-\frac{5}{7}\right)\right] = \frac{24336}{2401}$$

Arithmetic of Complex Numbers ($a+bi$)

$$i = \sqrt{-1}$$

$$\text{Ex. } (4-3i)(4-3i)$$

$$= 16 - 24i + \overset{-9}{9i^2}$$

$$= 7 - 24i$$

Never leave a power of i

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$

$$\text{Ex. } (3+2i)^4$$

$$= 3^4 + \binom{4}{1} 3^3 (2i)^1 + \binom{6}{2} 3^2 (2i)^2$$

$$+ \binom{4}{3} 3^1 (2i)^3 + (2i)^4$$

$$= \underline{81} + \underline{216i} - \underline{216} - \underline{96i} + \underline{16}$$

$$= -119 + 120i$$

$$\text{Ex. } (1 - i)^6$$

$$= 1^6 + \binom{6}{1} 1^5 (-i)^1 + \binom{6}{2} 1^4 (-i)^2 + \binom{6}{3} 1^3 (-i)^3 + \binom{6}{4} 1^2 (-i)^4 + \binom{6}{5} 1^1 (-i)^5 + (-i)^6$$

$i^6 = i^4 \cdot i^2$

$$= \cancel{1} - 6i - \cancel{15} + 20i + \cancel{15} - 6i - \cancel{1}$$

$$= 8i$$

$$\text{Ex. } \frac{2+i}{1-i} \cdot \frac{1+i}{1+i} = \frac{2+3i-1}{1+1}$$

$$= \frac{1+3i}{2} = \frac{1}{2} + \frac{3}{2}i$$

Ex- Find $\sqrt{3+4i}$

$$\sqrt{3+4i} = a + bi$$

$$3+4i = a^2 + 2abi - b^2$$

$$3+4i = (a^2 - b^2) + (2ab)i$$

$$\begin{cases} 3 = a^2 - b^2 \\ 4 = 2ab \end{cases} \rightarrow a = \frac{2}{b}$$

$$3 = \left(\frac{2}{b}\right)^2 - b^2$$

$$3 = \frac{4}{b^2} - b^2$$

$$3b^2 = 4 - b^4$$

$$b^4 + 3b^2 - 4 = 0$$
$$(b^2 + 4)(b^2 - 1) = 0$$

no reals

$$\downarrow$$
$$b = 1 \text{ or } b = -1$$
$$a = 2 \text{ or } a = -2$$

$$\sqrt{3+4i} = 2+i \text{ or } -2-i$$

Ex. Solve for $a+ib$

$$\frac{(2+i)(a+ib)}{2+i} = \frac{11-2i}{2+i} \cdot \frac{2-i}{2-i}$$

$$a+ib = \frac{20}{5} - \frac{15i}{5}$$

$a = 4$
 $b = \frac{-15}{5} = -3$

HW

3C retry b-g
as needed

3D #1

3E #1c, g

3F #1cd

#2b

#3cd

3G #3b

c

