

Set 011 The “Big Five” Derivative Rules – Sum, Power, Product, Quotient, and Chain

[1 – 20] Find the derivative of each function. Factor whenever possible. Do not leave negative exponents.

[1]  $f(x) = e^2$

[2]  $f(t) = 1 - 4t$

[3]  $f(y) = 4y^2 - 3y + 2$

[4]  $y = \sqrt{3x}$

[5]  $r = \cos 3\theta$

[6]  $r = 3 \cos \theta$

[7]  $r = \cos^3 \theta$

[8]  $r = \cos \theta^3$

[9]  $r = \cos^3 \theta^2$

[10]  $r = \frac{1}{\sin \theta + \cos \theta}$

[11]  $v(t) = \frac{3t - 4}{5t + 1}$

[12]  $v(t) = \frac{(2t + 3)^4}{(3t + 1)^3}$

[13]  $a(t) = \frac{\cos t}{t \cdot e^t}$

[14]  $A(y) = y^2 \cdot \sec^2 y$

[15]  $f(z) = \frac{\pi}{2} e^{-\frac{1}{2}z^2}$

[16]  $x(t) = \frac{1}{\sqrt{t^2 + t + 1}}$

[17]  $y(t) = \tan(e^{2t})$

[18]  $f(x) = \sec^2 x - \tan^2 x$

[19]  $y(t) = \sin t \cdot e^{\sin t}$

[20]  $f(x) = x^5 (2x + 4)^6$

[21] [a] Find an equation for the tangent line to  $y = \sin^2 x$  at  $x = \frac{\pi}{6}$ .

[b] (CALCULATOR) Use the tangent line to approximate  $y\left(\frac{1}{2}\right)$ . Find the percent error in this approximation.

[c] Find an equation for the normal line to  $y = \sin^2 x$  at  $x = \frac{\pi}{4}$ .

[22] [a] Find an equation for the tangent line to  $f(t) = e^t$  at  $t = 0$ .

[b] (CALCULATOR) Use the tangent line to approximate  $f(-0.2)$ . Find the percent error in this approximation.

[c] Find an equation for the normal line to  $f(t) = e^t$  at  $t = 1$ .

[23] [a] Find an equation for the tangent line to  $f(x) = \frac{x + 5}{x + 1}$  at  $x = 1$ .

[b] (CALCULATOR) Use the tangent line to approximate  $f(1.2)$ . Find the percent error in this approximation.

[c] Find an equation for the normal line to  $f(t) = e^t$  at  $t = 1$ .